

# kinematics equations

## UNIT 2 and 3 CP EQUATIONS

Var	Given value	Units	Description
$\Delta x$		m	displacement
$x_f$		m	final position
$x_i$		m	initial position
<i>speed</i> <sub>ave</sub>		$\frac{m}{s}$	average speed
$d$		m	distance
$t$		s	time
$v_{ave}$		$\frac{m}{s}$	average velocity
$\Delta v$		$\frac{m}{s}$	change in velocity
$v_f$		$\frac{m}{s}$	final velocity
$v_i$		$\frac{m}{s}$	initial velocity
$a$		$\frac{m}{s^2}$	acceleration

$$\Delta x = x_f - x_i$$

$$speed_{ave} = \frac{d}{t}$$

$$v_{ave} = \frac{\Delta x}{t}$$

$$\Delta v = v_f - v_i$$

**kinematics equations (continued)**

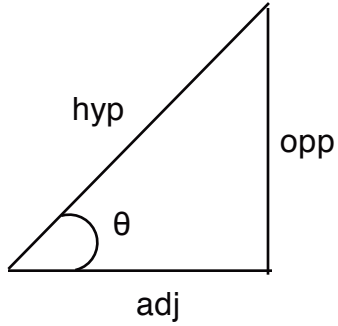
$$a = \frac{\Delta v}{t}$$

$$v_f = v_i + at$$

$$\Delta x = \frac{1}{2} a t^2$$

# dynamics equations

## UNIT 4 and 5 CP EQUATIONS



Remember! SOH CAH TOA

Var	Given value	Units	Description
$\theta$		$^\circ$	angle in degrees
<i>opp</i>			side opposite of angle
<i>hyp</i>			longest side of a right triangle
<i>adj</i>			side adjacent to angle

$$\sin \theta = \frac{opp}{hyp}$$

$$\cos \theta = \frac{adj}{hyp}$$

$$\tan \theta = \frac{opp}{adj}$$

**dynamics equations (continued)**

Var	Given value	Units	Description
<i>weight</i>		N	force of gravity on object
<i>m</i>		kg	mass
<i>g</i>	10	$\frac{\text{m}}{\text{s}^2}$	acceleration due to gravity
$F_{\text{NET}}$		N	net or total force
<i>a</i>		$\frac{\text{m}}{\text{s}^2}$	acceleration
<i>f</i>		N	force of friction
$\mu$			coefficient of friction
<i>N</i>		N	normal force

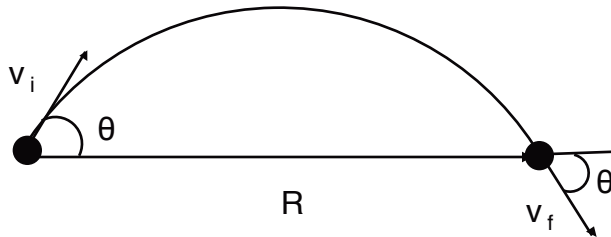
$$\textit{weight} = m g$$

$$F_{\text{NET}} = m a$$

$$f = \mu N$$

# projectile and circular motion equations

UNIT 6 and 8 CP EQUATIONS



Var	Given value	Units	Description
$R$		m	range of a projectile
$V_i$		$\frac{m}{s}$	launch velocity of a projectile
$V_f$		$\frac{m}{s}$	impact velocity of a projectile
$g$	10	$\frac{m}{s^2}$	acceleration due to gravity
$\theta$		$^{\circ}$	launch angle with respect to the horizontal

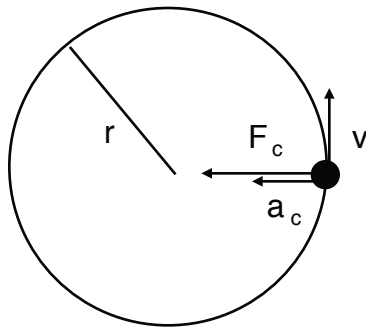
$$V_i = V_f$$

$$time_{up} = time_{down}$$

$$R = \left( \frac{v_i^2}{g} \right) \sin(2\theta)$$

## projectile and circular motion equations (continued)

Var	Given value	Units	Description
$v$		$\frac{m}{s}$	tangential velocity or linear speed
$r$		m	radius of circular path
$T$		s	period – time to go around circle once
$a_c$		$\frac{m}{s^2}$	centripetal acceleration
$F_c$		N	centripetal force – net force towards the center of the circle
$m$		kg	mass



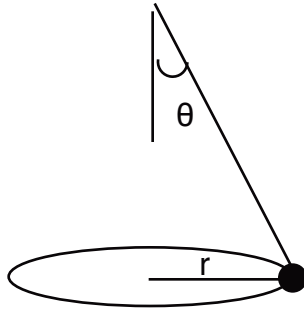
$$v = \frac{2\pi r}{T}$$

$$a_c = \frac{v^2}{R}$$

$$F_c = m a_c$$

## projectile and circular motion equations (continued)

This formula is for a conical pendulum aka the Flying Pig!



Var	Given value	Units	Description
$\theta$		$^{\circ}$	angle string makes with the vertical

$$\tan \theta = \frac{v^2}{rg}$$

## work and energy equations

### UNIT 7 CP EQUATIONS

Var	Given value	Units	Description
<i>work</i>		J	work
<i>F</i>		N	force in the direction of $\Delta x$
$\Delta x$		m	displacement
$\Delta E$		J	change in energy of a system
$E_g$		J	gravitational potential energy
<i>m</i>		kg	mass
<i>g</i>	10	$\frac{m}{s^2}$	acceleration due to gravity
<i>h</i>		m	height above reference point
$E_k$		J	kinetic energy
$E_{el}$		J	elastic potential energy
<i>k</i>		$\frac{N}{m}$	spring constant
$\Delta x_s$		m	amount spring is stretched
$F_s$		N	force required to stretch a spring
<i>power</i>		W	power, the rate at which work is done
<i>t</i>		t	time
<i>v</i>		$\frac{m}{s}$	velocity

$$work = \Delta E$$

$$work = \text{area under } F \text{ vs } \Delta x \text{ curve}$$



**work and energy equations (continued)**

$$work = F\Delta x$$

$$E_g = mgh$$

$$E_k = \frac{1}{2}mv^2$$

$$E_{el} = \frac{1}{2}k\Delta x_s^2$$

$$F_s = k\Delta x_s$$

$$power = \frac{work}{t}$$

$$power = Fv$$

## momentum equations

Var	Given value	Units	Description
$p$		$\frac{\text{kg m}}{\text{s}}$	momentum
$m$		kg	mass
$v$		$\frac{\text{m}}{\text{s}}$	velocity
<i>impulse</i>		Ns	impuse
$F$		N	applied force
$t$		s	time
$\Delta p$		$\frac{\text{kgm}}{\text{s}}$	change in momentum
$v_f$		$\frac{\text{m}}{\text{s}}$	final velocity
$v_i$		$\frac{\text{m}}{\text{s}}$	initial velocity

$$p = m v$$

$$\textit{impulse} = F t$$

$$\textit{impulse} = \Delta p$$

$$\Delta p = m(v_f - v_i)$$

## momentum equations (continued)

conservation of momentum for a system of two objects (sum of initial momenta = sum of final momenta)

$$m_1 v_{1i} + m_2 v_{2i} = m_1 v_{1f} + m_2 v_{2f}$$

For an elastic collision, kinetic energy is also conserved.

$$\text{sum of } E_{ki} = \text{sum of } E_{kf}$$

For a completely inelastic collision where objects stick together after collision:

$$m_1 v_{1i} + m_2 v_{2i} = (m_1 + m_2) v_f$$

conservation of momentum for an explosion (like firing a gun) where the system was initially at rest:

$$0 = m_1 v_{1f} + m_2 v_{2f}$$